

$$\exp h(\alpha \cup X) - h(\alpha) = \frac{\alpha_i + n_i}{\sum_i \alpha_i + n_i}$$